

# Point Processes and Spatiotemporal Modeling of Alphabet Spread in Ancient Italy



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DataX Stacks Xchange

# Overview

- 1 Introduction
- 2 The Data and Data Collection Problems/Procedures
- 3 Determining Alphabet Distinctions
- 4 The Model
- 5 Results and Interpretation

# What languages are attested in the inscriptional record in 1<sup>st</sup> millennium BCE Italy?



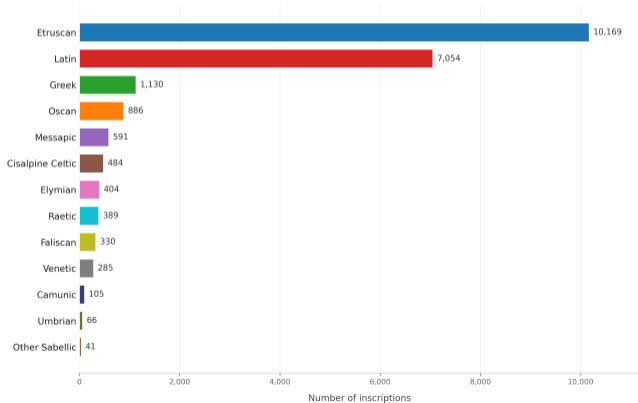
# Languages attested in the inscriptional record in 1st millennium BCE Italy

A. Language map of ancient Italy

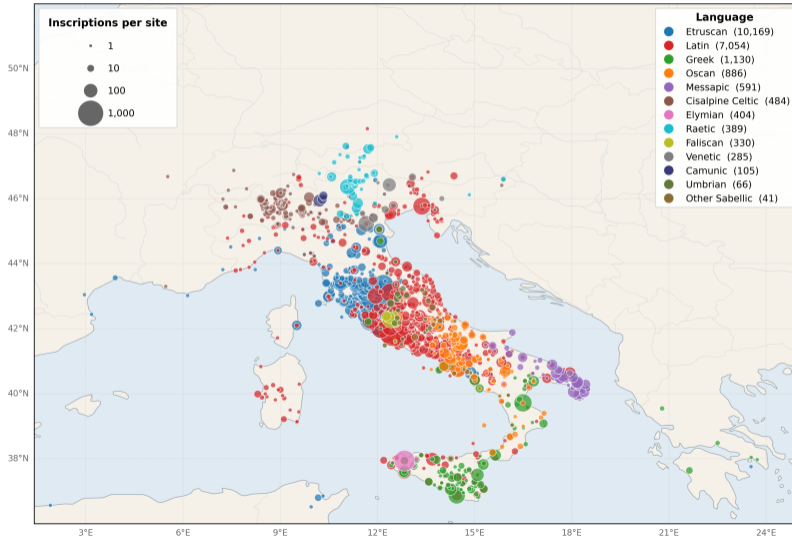


Wallace 2007:x

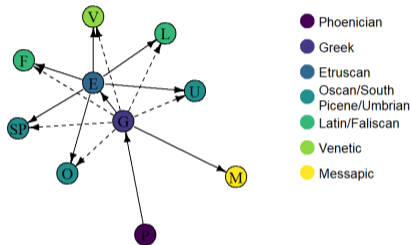
B. Language distribution in the dataset



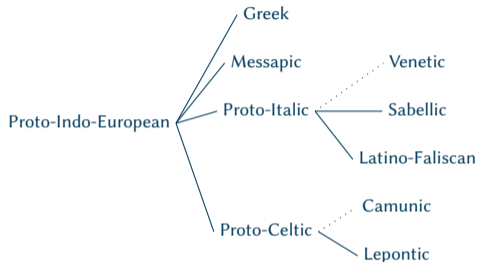
# Spatial distribution of languages in the epigraphic record



# Linguistic relationships vs. alphabet relationships



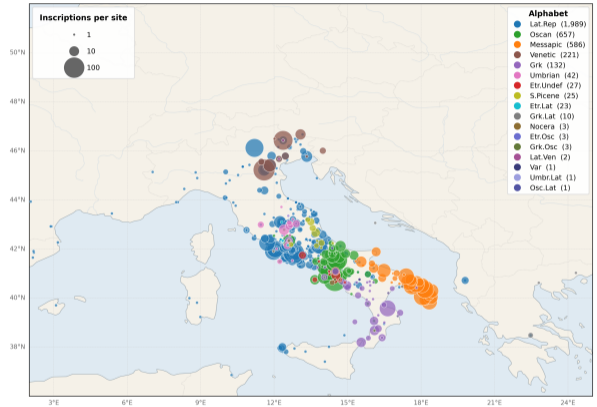
Generally accepted direction of alphabet spread in Italy



Phylogeny of Indo-European languages in Ancient Italy

# The need for a new dataset

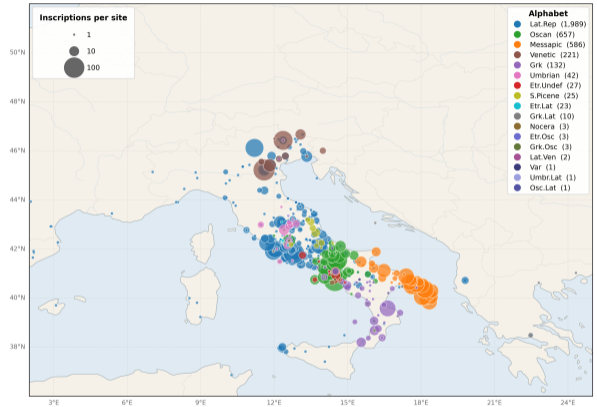
- Reuben Pitts published the *Corpus of the Epigraphy of the Italian Peninsula in the 1st Millennium BCE (CEIPoM)* in 2022



Alphabet heatmap from Pitts' 3,868-inscription dataset for 1<sup>st</sup>-millennium BCE Italy

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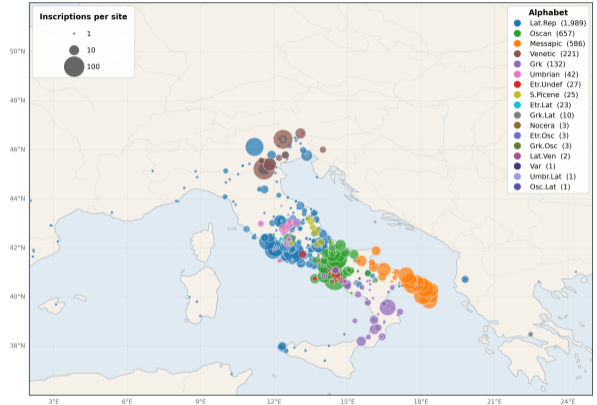
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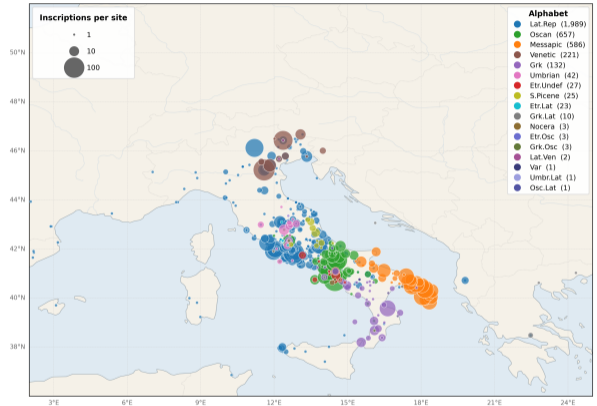
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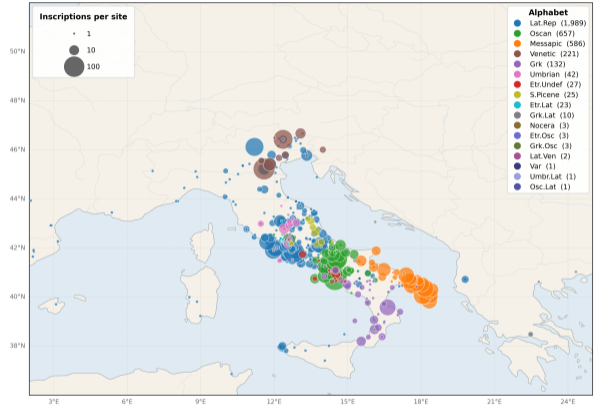
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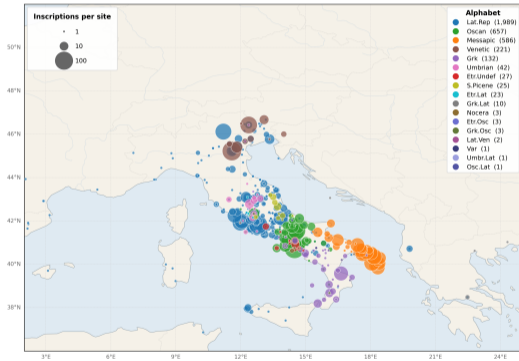
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- Notable errors, including Etruscan and Hernican inscriptions in Anagni listed as Oscan language and alphabet



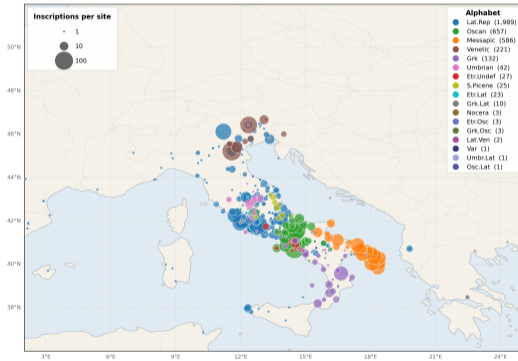
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# Comparison of alphabets in the epigraphic record between databases



Pitts' 3,868-inscription dataset

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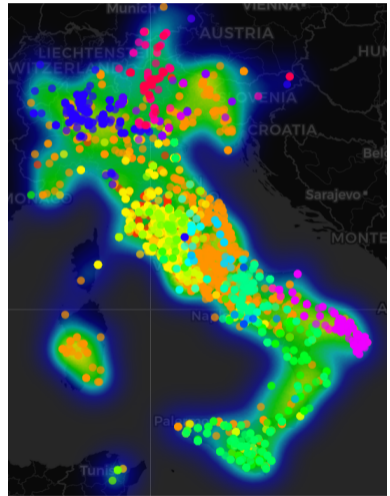
Pitts' 3,868-inscription dataset



Current 21,937 inscription dataset

## Data collection for the model: variables

- Each row  $i$  in the corpus encodes the attestation of one *inscription event*.
- We record five attributes for every inscription:
  - `Date.Start`, `Date.End` (calendar years)
  - `Latitude`, `Longitude` (decimal degrees)
  - `Alphabet` (integer label, e.g. 1 = S.Etruscan)
  - `Region`
  - `Object.Type` (genre)
  - `Site_Id` derived from rounded (lat, lon)
  - Fields under construction for further analyses:
    - Archaeological Context (including whether or not it exists), `Inscription.Type`, `Alphabet.Direction`, `Character.States.for.Individual.Letters`



Spatial density of all inscriptions

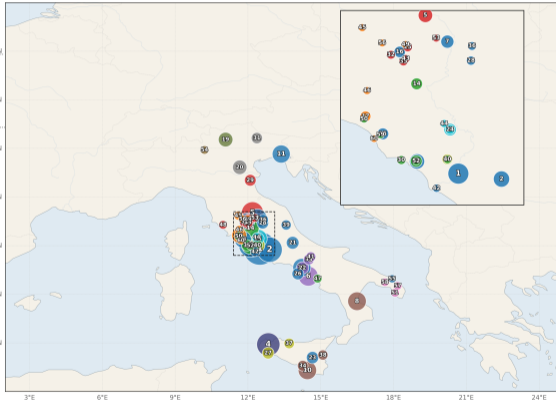
## Data collection for the model: major editions and databases consulted

Language	Primary Edition(s) Used	Database(s) Used
Etruscan	Rix and Meiser 2014	N/A
Greek	Dubois 1989, 1995, 2002, 2008	I.Sicily
Latin	<i>CIL</i> I <sup>2</sup> , III, VI, XI	<i>CEIPoM</i> , <i>EDCS</i>
Elymian	Agostiniano 1977, 2021	I.Sicily
Raetic	Volumes cited in <i>TIR</i>	<i>TIR</i>
Lepontic	Volumes cited in <i>Lexicon Leponticum</i>	<i>Lexicon Leponticum</i>
Cisalpine Gaulish	Volumes cited in <i>Lexicon Leponticum</i>	<i>Lexicon Leponticum</i>
Sabellic Languages	Crawford et al. 2011, Rix 2002	<i>CEIPoM</i>
Faliscan	Bakkum 2009	<i>CEIPoM</i>
Messapic	De Simone and Marchesini 2002	<i>CEIPoM</i>
Camunic	Tibiletti Bruno 1990, Prosdocimi 1965	N/A
Venetic	Lejeune 1974, Prosdocimi and Pellegrini 1967	<i>CEIPoM</i>

# Alphabet distribution: major epigraphic centers (N ≥ 50)

## Sites by inscription count

- |                                      |                               |
|--------------------------------------|-------------------------------|
| 1 Roma                               | 20 Catubrium (Cadore)         |
| 2 Palestrina / Praeneste / Terracina |                               |
| 3 Cerveteri / Argylla / ...          | 18 Compocharo                 |
| 4 Segesta                            | 19 Gela                       |
| 5 Viareggio                          | 20 Ponticello di Campo        |
| 6 Pompei                             | 21 Assisi / Assisium          |
| 7 Perugia / Perusia                  | 22 Terni Inesere / ...        |
| 8 Bybaris                            | 23 Catania                    |
| 9 Valeri Viteres (Civ.)              | 24 Ascoli Piceno / Ascul...   |
| 10 Camarina                          | 25 Portonaccio                |
| 11 Aquilina                          | 26 Monte Vairano (found ...)  |
| 12 Capua / Cassilinum                | 27 Ostia Antica               |
| 13 Banditaccia                       | 28 Città della Pieve          |
| 14 Crocifisso del Tufo               | 29 Corchiano                  |
| 15 Tarquinia / Corneto               | 30 Asciano, T. d. Marconi     |
| 16 Chiusi / Clusium                  | 31 Sovana                     |
| 17 Area della Città                  | 32 Pontecagnano               |
| 18 Orvieto                           | 33 Arce                       |
| 19 Sanzeno                           | 34 Badia di S. Cristoforo     |
| 20 Anzio (Ester)                     | 35 Camposcala                 |
| 21 Corfinio / Pentima / ...          | 36 Avelinum (Aletio)          |
| 22 Capua                             | 37 Banditaccia, T. d. Iscr... |
| 23 ?                                 | 38 Pieve del Vesco            |
| 24 Valeri Viteres (Civ.)             | 39 Mancagnano                 |
| 25 Bruscampone                       | 40 Brindisi                   |
| 26 Cuma                              | 41 Minturno                   |
| 27 Castelvetrano / Selin...          | 42 Lupatone (Lecce)           |
| 28 Ravenna / Mevania                 | 43 Uria (Orta)                |
| 29 Valle Trebbia                     | 44 Montarozzi, Villa Tar...   |
| 30 Yrti                              | 45 Grevisca                   |



## Dominant alphabet

- Lat. Rep (16 sites)
- Etr. N (8 sites)
- Etr. S (8 sites)
- Etr. Undef (6 sites)
- Oscan (4 sites)
- Grik (4 sites)
- Messapic (3 sites)
- Faliscan (3 sites)
- Lat. Arc. (3 sites)
- Venetic (2 sites)
- Elymian (1 site)
- Raet. Sanz (1 site)
- Camunic (1 site)

## Inscriptions per site

- 50
- 100
- 250
- 500
- 1,000

# <F> in the Italic chat: distinguishing between alphabets used by different languages in the same area: Ager Faliscus



--- ilio · cesi · fī  
 --- x cania xx  
 --- a

CIE 8215 (Faliscan)



decon  
 a = f

CIE 8255 (Latin)



mi tafina lazia vilianas

CIE 8901 (South Etruscan)



[1] just before / 1 next / pe / redant / pl-1]

Bonus: *Imagines Italicae* Interamna Praetuttiorum 2  
 (South-Picene, not in Ager Faliscus)

## Distinguishing between alphabets used by the same language: Etruscan



REE 37:340.2; Bronze colander, Orvieto, 4th–3rd c. BCE;  
sinistroverse /fut<sup>h</sup>ina/ ‘tomb goods’



REE 51:271.176; Attic style vase, Cerveteri?, 5th c. BCE?



REE 69:388.84; Tomb inscription, Siena, after 400 BCE

**Table 14.1** Regional Spelling of the Sibilants (/s/ and /ʃ/) and the Velar Stop (/k/).

Regions	/s/	/ʃ/	/k/
Northern (Chiusi)	ʃ	ʃ	ʃ
Central (Tarquinia)	ʃ	ʃ	ʃ
Southern (Caere and Veii)	ʃ	ʃ	ʃ

Wallace 2016:206; exceptions are common; Veii also has X /s/ 13 / 48

# Distinguishing between alphabets used by the same language: Raetic

	alpha	epsilon	waw	zeta	heta	theta	iota	kappa	lambda	mu
M	Α	ϵ	Ϝ	Ζ	Η	Θ	Ι	Κ	Λ	Μ
S	Λ	ϵ	Ϝ	—	Η	Χ	Ι	Κ	↓	ϣ
	<i>a</i>	<i>e</i>	<i>v</i>	<i>z</i>	<i>h</i>	<i>θ</i>	<i>i</i>	<i>k</i>	<i>l</i>	<i>m</i>

	nu	pi	san	rho	sigma	tau	/tʰ/	upsilon	phi	chi
M	ν	π	Μ	ρ	ς	τ	τʰ	υ	φ	χ
S	ν	π	Μ	ρ	ς	τ	↑	υ	φ	χ
	<i>n</i>	<i>p</i>	<i>s</i>	<i>r</i>	<i>s</i>	<i>t</i>	<i>β</i>	<i>u</i>	<i>φ</i>	<i>χ</i>

Table 1. The characters of the Magrè (M) and Sanzeno (S) alphabets (standardised and sinistroversive) with transliteration letters.

ϜϜΑΠΥ

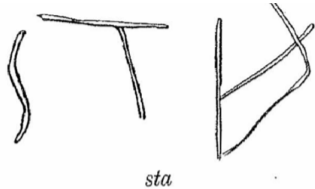
Ϝ↓ΛΥΥ

Figure: Distinctions of the two primary Raetic alphabets from Salomon 2020. The sequence *-nuale* from two inscriptions; characters from *Thesaurus Inscriptionum Raeticarum*

# Encoding problems: short inscriptions



*Lexicon Leponticum* BG-28.1: /pit/ or /lit/?



CIE 8013 (Ager Faliscus); Latin or Faliscan?

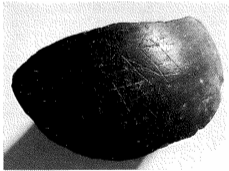


Fig. 2. Anagni, S. Cecilia: graffito n. 2.

Colonna and Gatti 1990: /hasu/ or /haθu/?



*Thesaurus Inscriptionum Raeticarum* SZ-04: is this an <X> or a non-linguistic design?

## Research questions

- Broadest level: linguistic (e.g., Indo-European vs. non-Indo-European, Celtic vs. Italic, Latin vs. Sabellic) and geographic (e.g., Latium vs. Magna Graecia vs. Sicily vs. Cisalpine Gaul) categories have been adopted as conventional ways to divide the material of ancient Italy (in part to keep print volumes shorter): **to what degree do these divisions inhibit our ability to understand alphabet spread in ancient Italy?**

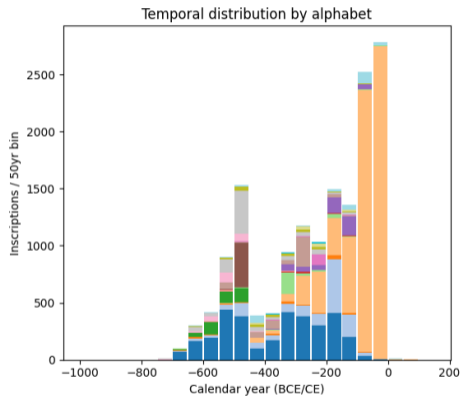
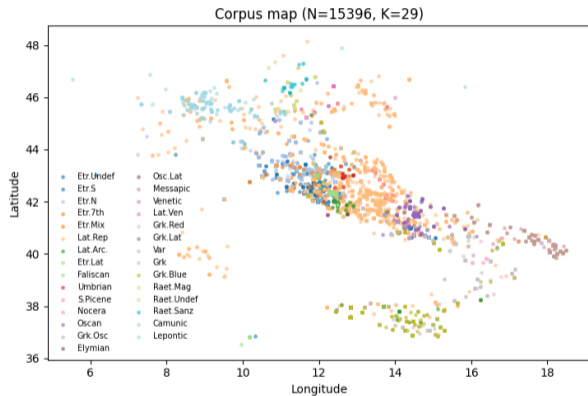
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- **Latin** is often invoked to explain alphabet distribution changes in the final 2 centuries BCE (e.g., De Simone and Marchesini 2002; Wallace 2007; Wallace 2008): **is there a monolithic response to Roman conquest, or are narratives of (alphabetic) resistance lost in this narrative?**

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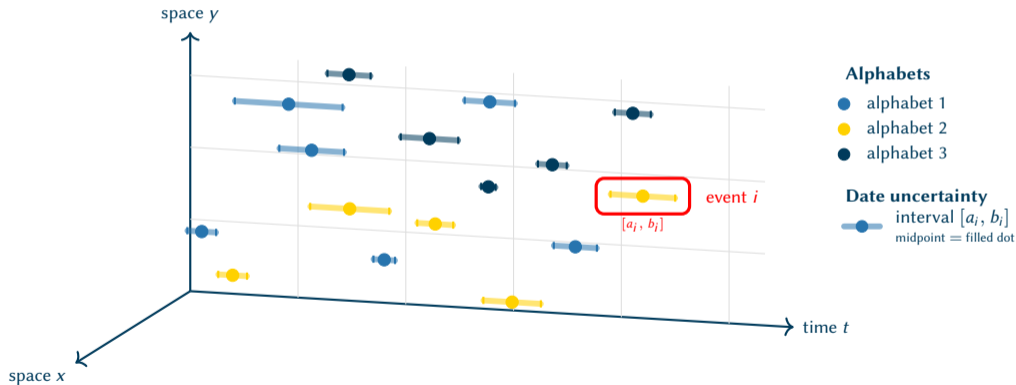
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- When moving outside the Greco-Roman lens of classics, **what new insights into diffusion and community interactions in 1<sup>st</sup> millennium BCE can be inferred from the inscriptional record?**

# Corpus data for modeling



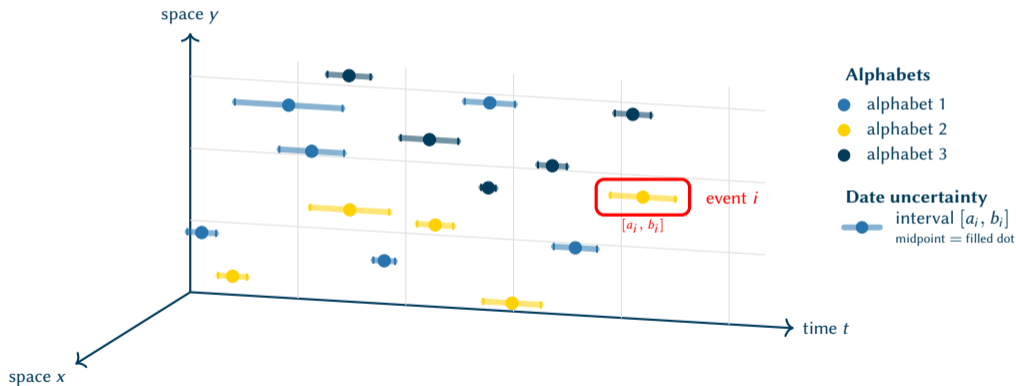
# Marked Point Process modeling of alphabet dynamics

Each inscription is a *point in space-time*, marked with an alphabet. The date is rarely known exactly — it's an *interval*  $[a_i, b_i]$ .



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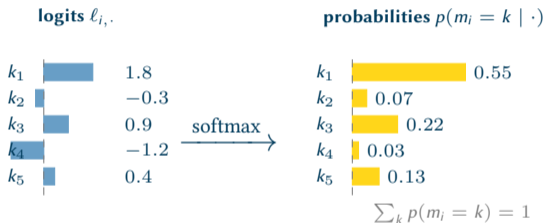
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- For each event  $i$ : given location, time interval, and the alphabets of nearby earlier events, what's the probability  $i$  is in alphabet  $k$ ?

# A Probability Vector via Softmax

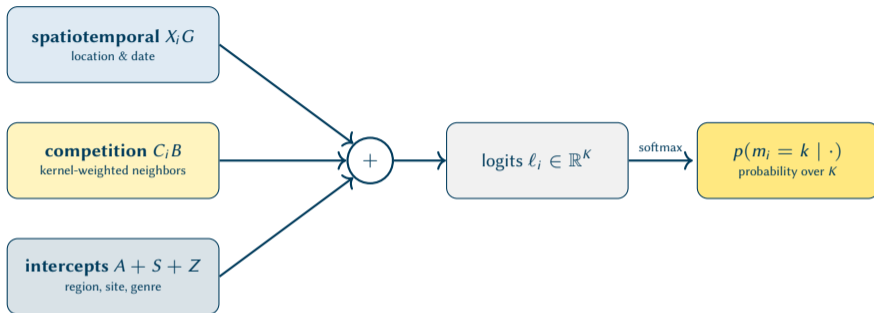
- For event  $i$ , we calculate the log-odds  $K$  of the inscription being written in a given alphabet.
- We turn these into probabilities using a softmax function.



$$p(m_i = k) = \frac{\exp(\ell_{i,k})}{\sum_{j=1}^K \exp(\ell_{i,j})}$$

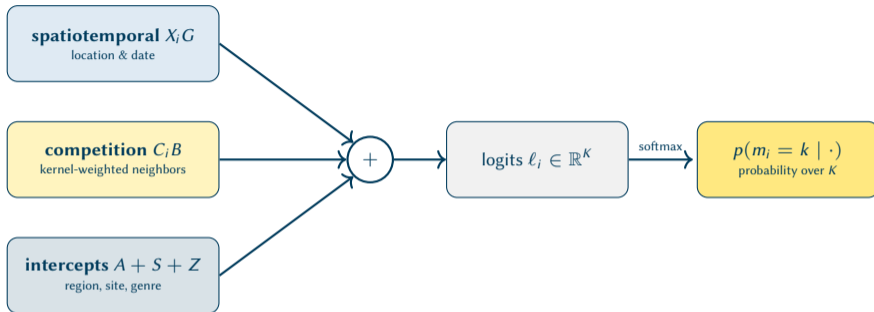
The modeling problem is essentially: **how do we build the logit vector  $\ell_i$  for each event?**

## Visualizing the model



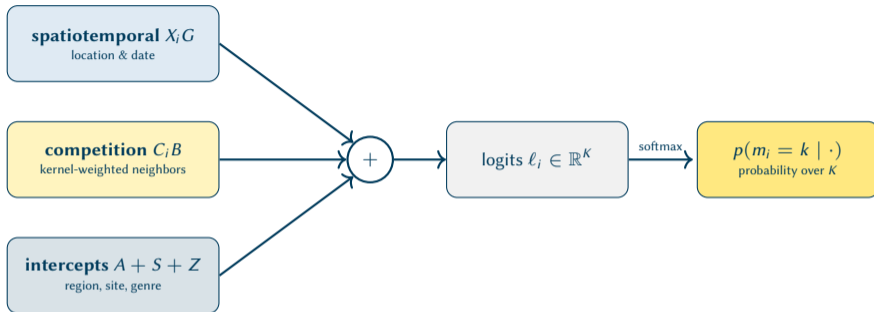
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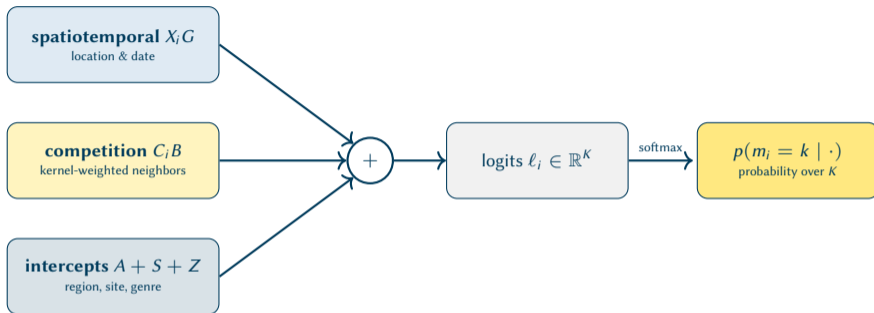
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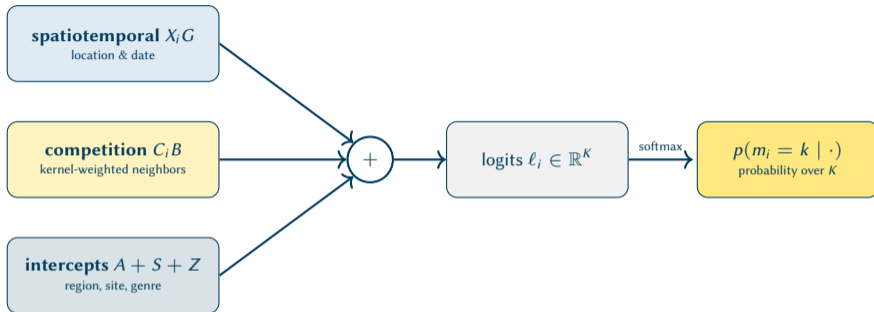
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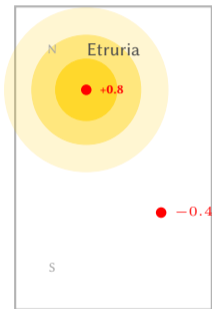
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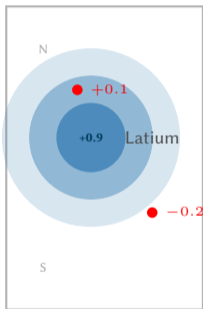


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  - **Intercepts**: what is the *baseline* for this region/site/genre?
- 2 We interpret the competition matrix  $B$  as cross-alphabet contact after accounting for the variation explained by location, time, region, site, and object type (genre).

# The spatiotemporal effect $X_i G$ – “Where and when is each alphabet localized?”







**Etruscan** spatiotemporal basis  
5<sup>th</sup>-c. BCE



**Latin** spatiotemporal  
1<sup>st</sup>-c. BCE

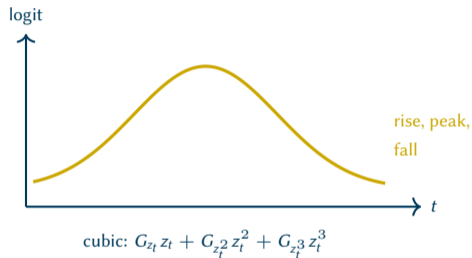
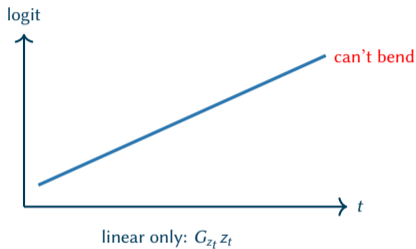
## Key

-  favored zone ( $X_i G > 0$ )
-  neutral ( $X_i G \approx 0$ )
-  one event  $i$
-  **+0.8** spatiotemporal basis logit at  $i$

**Interpretation:** Given only event  $i$ 's location and date, how much does this place-and-time *favor* each alphabet? The model learns one such surface per alphabet, parameterized as a low-order polynomial in  $(x, y, t)$ .

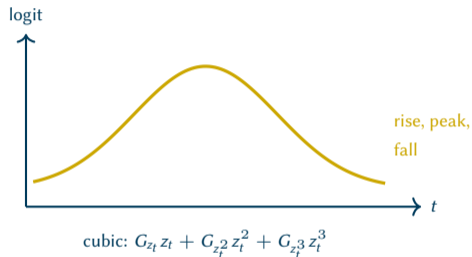
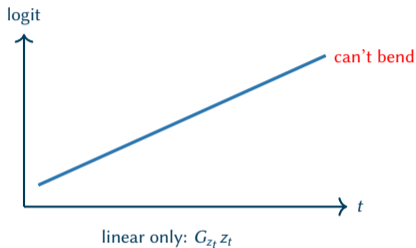
## Modeling time as a cubic polynomial

Alphabet usage isn't linear in time. Most alphabets in this corpus *rise, peak, and decline*. A linear time feature alone can't produce a "bendy" trend.



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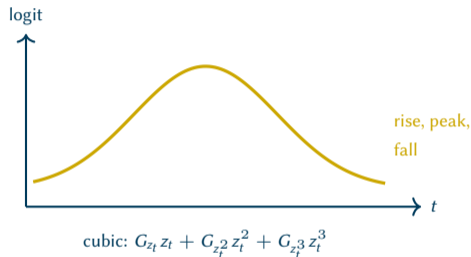
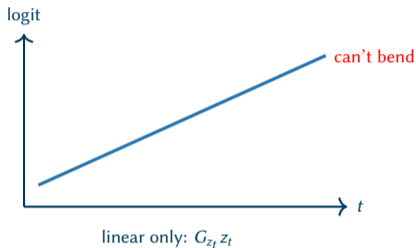
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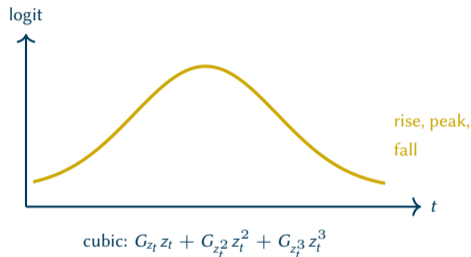
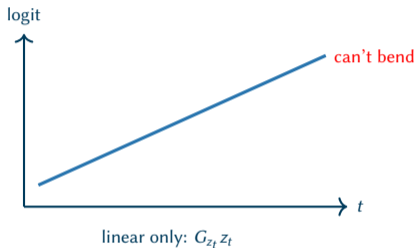
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- **Latin** is rare early, grows through the Republic, and dominates late.
- **Etruscan** grows, peaks around the 4<sup>th</sup>-3<sup>rd</sup> c. BCE, then declines. A cubic polynomial in  $z_t$  can capture both.

## Modeling time as a cubic polynomial

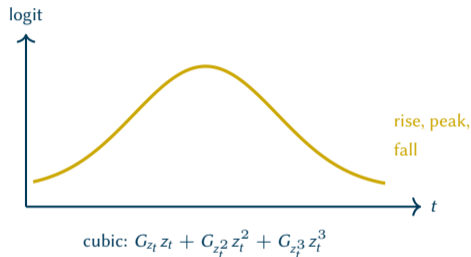
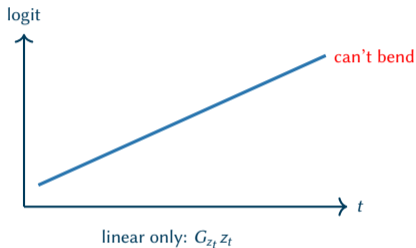
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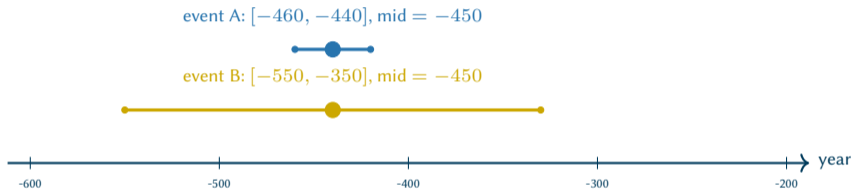
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- How do we compute  $z_t^n$  when the date is an *interval*, not a point?

## Date Uncertainty: The Problem

Every inscription comes with a date *range*  $[a_i, b_i]$ , not a point. Using just the midpoint discards information about how confident we are.

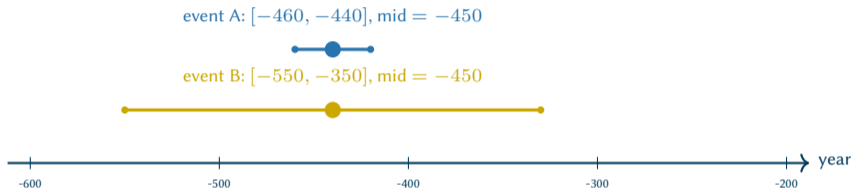


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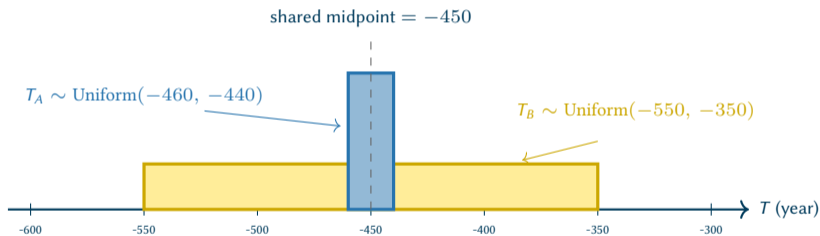


**Both events have a midpoint of  $-450$ .**

- Midpoint-only treatment says they are *identical* on the time axis.
- But event B carries far more uncertainty about *when* the text was actually inscribed.

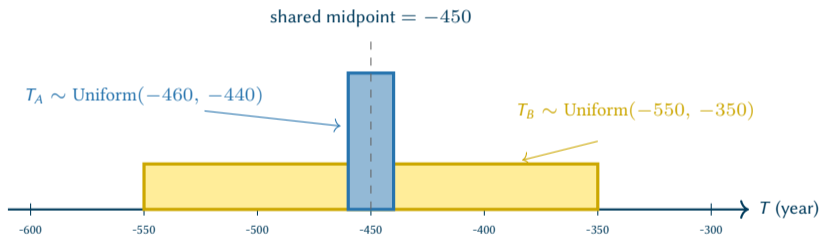
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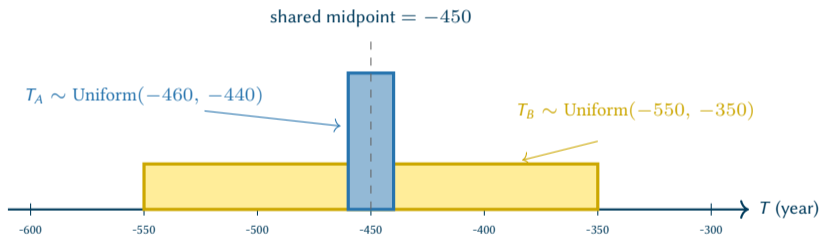
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- Both distributions are centered at  $-450$ . But event A's mass is concentrated; event B's mass is spread.
- Instead of plugging in the midpoint and *then* raising it to the  $n$ -th power for the  $z_t^n$  polynomial, we ask: what is the *expected* value of  $T^n$  under each distribution?

## Using moments to define the cubic date terms

For  $T \sim \text{Uniform}(a, b)$ , the first three raw moments have closed forms:

$$\mathbb{E}[T] = \frac{a+b}{2}, \quad \mathbb{E}[T^2] = \frac{a^2 + ab + b^2}{3}, \quad \mathbb{E}[T^3] = \frac{a^3 + a^2b + ab^2 + b^3}{4}$$

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For event A (low uncertainty) and event B (high uncertainty),  $\mathbb{E}[T]$  is the same. But  $\mathbb{E}[T^2]$  and  $\mathbb{E}[T^3]$  are not.

	$\mathbb{E}[T]$	$\mathbb{E}[T^2]$	$\mathbb{E}[T^3]$
Event A: [-460, -440]	-450	<b>202,533</b>	<b>-91,170,000</b>
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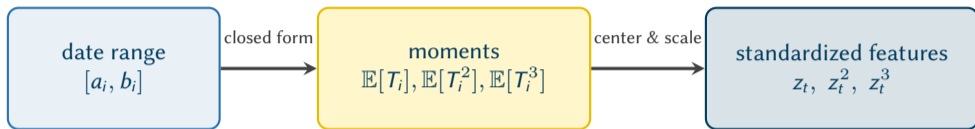
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The difference  $\mathbb{E}[T^2] - (\mathbb{E}[T])^2 = \text{Var}(T) = \frac{(b-a)^2}{12}$  is the uncertainty signal. Wider date range  $\Rightarrow$  larger gap  $\Rightarrow$  different  $z_t^2$  feature value.

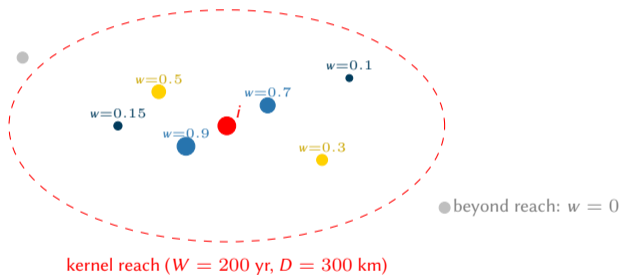
## Plugging the Moments into the Design Matrix



- Using moments allows us to model the difference between an inscription that has lower date uncertainty than one with a higher date uncertainty.

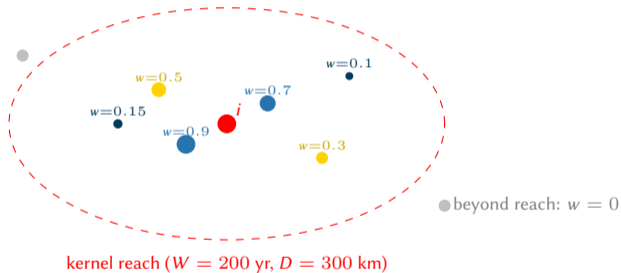
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First we build  $C_i$ : a probability vector saying *what fraction of event  $i$ 's recent local neighborhood used each alphabet.*



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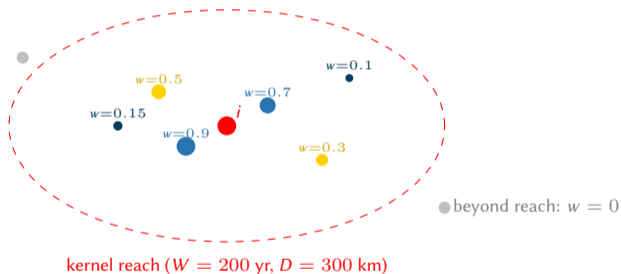


Each earlier neighbor  $j$  gets a weight  $w_{ij} = \underbrace{\exp(-\beta (t_i - t_j))}_{\text{exponential in time}} \cdot \underbrace{\exp(-\frac{1}{2}|\mathbf{0r}_i - \mathbf{r}_j|^2/\sigma^2)}_{\text{Gaussian in space}}.$

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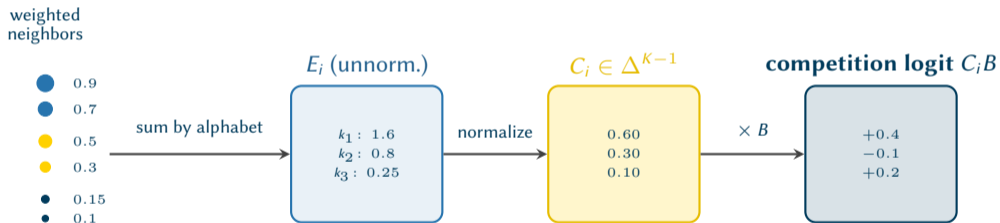


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- Closer in time *and* space  $\Rightarrow$  larger weight.
- The kernel parameters  $(\beta, \sigma)$  are themselves learned from the data.

# The Competition $C_i B$ – What alphabets do neighboring inscriptions use: Part II

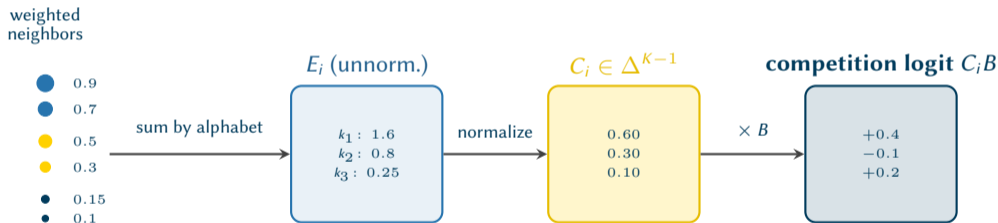
Sum the weights by alphabet, normalize  $\Rightarrow C_i$ . Then  $C_i B$  scores each alphabet by how favorably its mix of neighbors influences it.



- $C_i$ : What alphabets are around me, kernel-weighted?

# The Competition $C_i B$ – What alphabets do neighboring inscriptions use: Part II

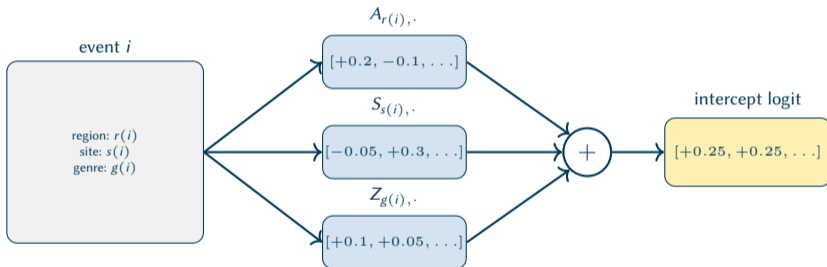
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- $C_i$ : What alphabets are around me, kernel-weighted?
- $B_{k \rightarrow j}$ : Given a neighbor wrote in  $k$ , how much does that push me toward writing in  $j$ ?

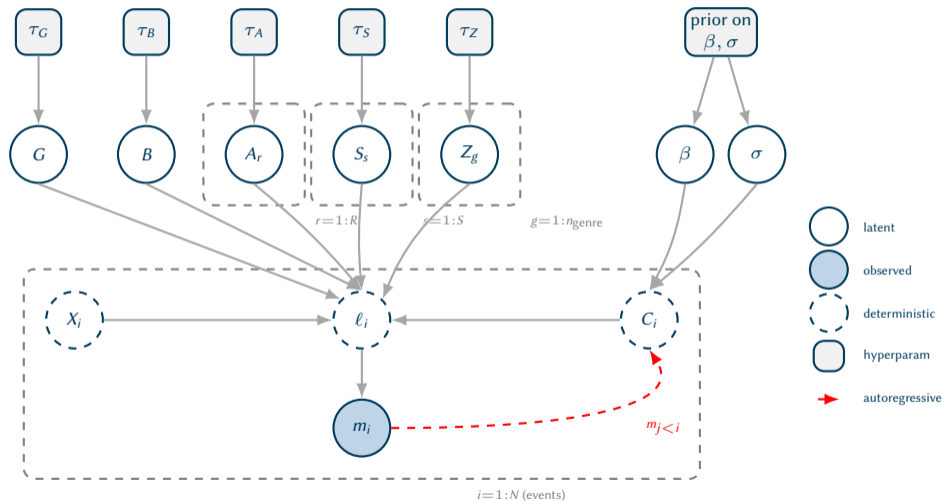
## Hierarchical intercepts: Defining baseline propensities by inscription attributes

Three additional parameters that absorb everything not captured by location, time, or the neighborhood.



- $A_{r,\cdot}$  — a  $K$ -vector per region (Etruria, Latium, Apulia, ...): captures region-wide baselines.
- $S_{s,\cdot}$  — a  $K$ -vector per site: captures single-find-spot idiosyncrasies (one tomb, one sanctuary).
- $Z_{g,\cdot}$  — a  $K$ -vector per genre (funerary, votive, ownership-mark, ...): captures genre-specific script preferences.

## Graphical representation of the model



# Inferring model parameters with Stochastic Variational Inference

The model has  $\sim 10^3$ – $10^4$  latent parameters (depending on the random effect structure).

## Inference Algorithm: SVI

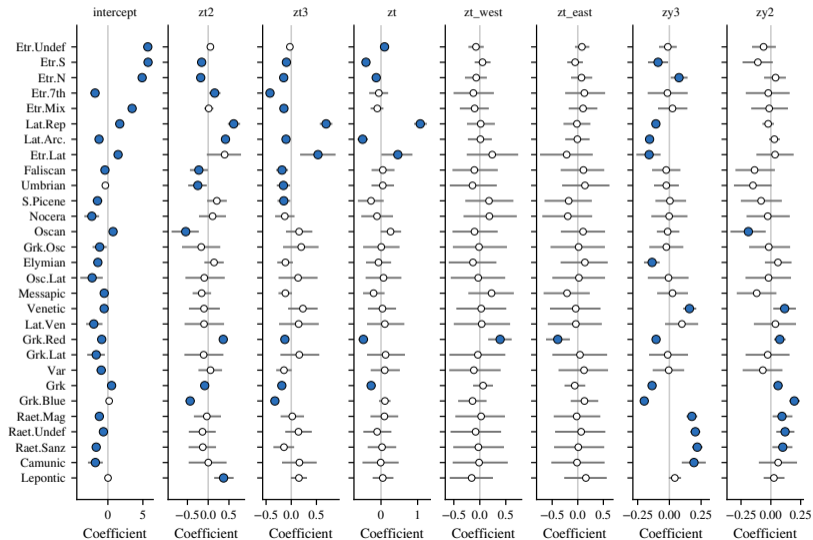
- **Guide:** AutoLowRankMultivariateNormal, rank 32.
- **Optimizer:** AdamW with warmup-cosine LR ( $5 \times 10^{-3}$  peak).
- **Process:** 10,000 steps | 4 particles per step | clipped gradients.

## Motivating the use of SVI

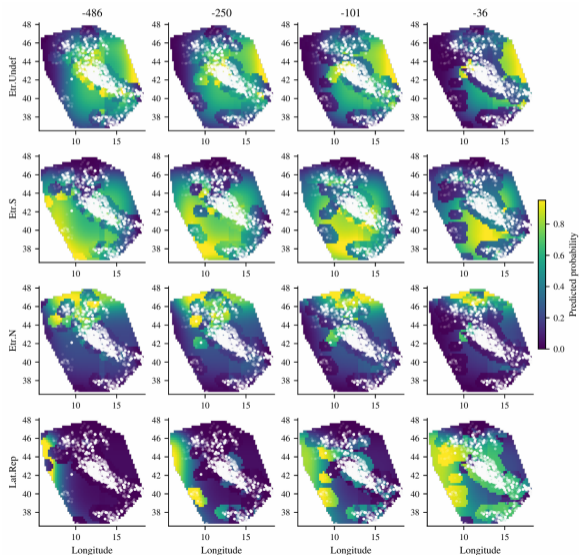
The geometry of  $B$  + the sparse edge graph + the kernel parameters makes Monte Carlo sampling methods slow at this scale.

⇒ **SVI gives us competitive posterior intervals**, at a fraction of the cost of sampling.

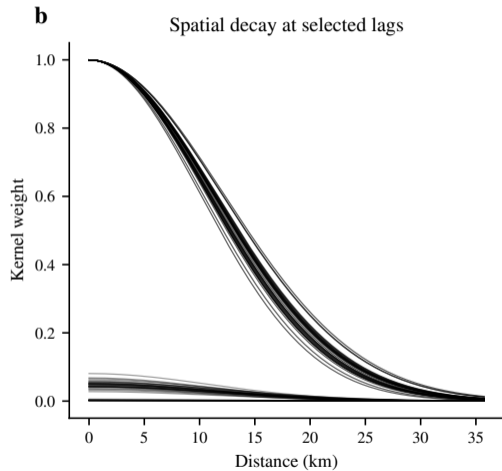
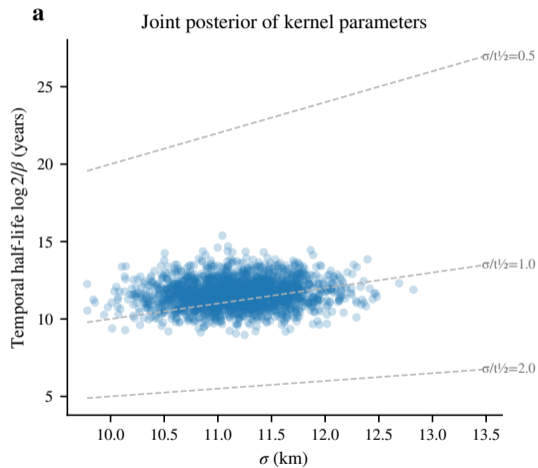
# Spatiotemporal coefficients



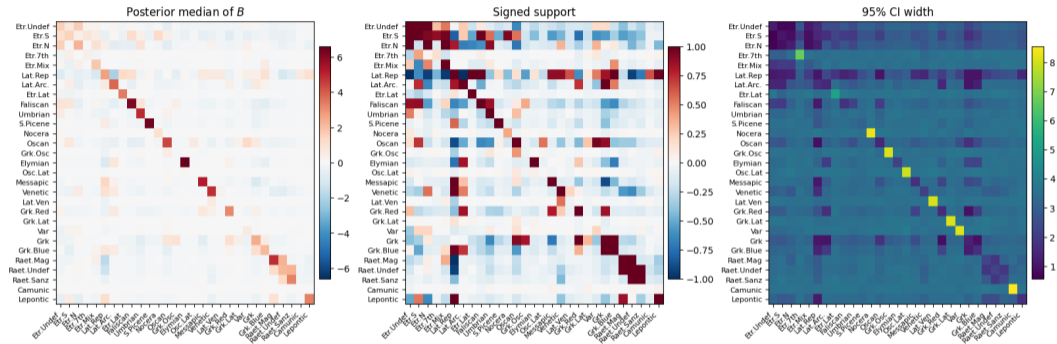
# Spatiotemporal probability fields for selected alphabets



# Kernel parameters

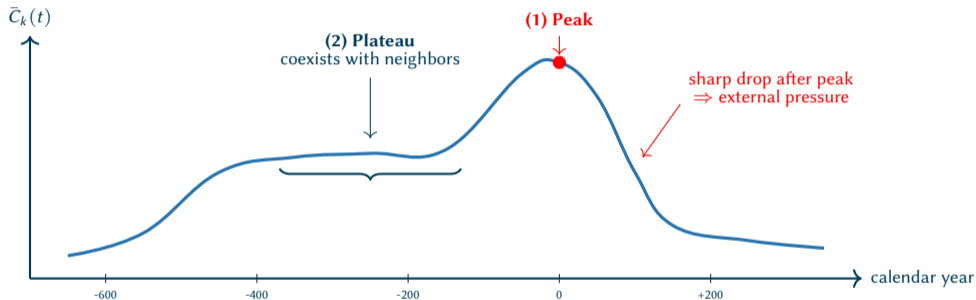


# Competition effect posteriors



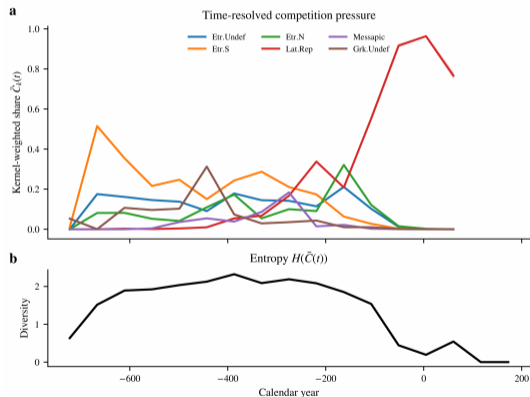
# Change in competition pressures

Each curve shows  $\bar{C}_k(t)$  for one alphabet  $k$ . Three things to look for:

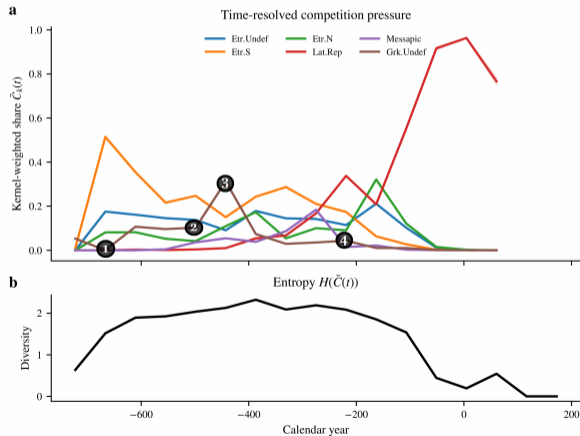


**Interpretation:**  $\bar{C}_k(t)$  is a kernel-weighted *share* of the neighborhood, which is robust to overall inscription rates and recovery bias.

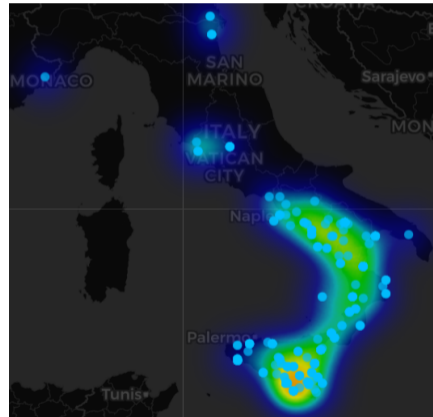
# Interpreting Alphabet Competition Over Time: Historical Events and Data Bias



# Interpreting Alphabet Competition Over Time: Greek Alphabet

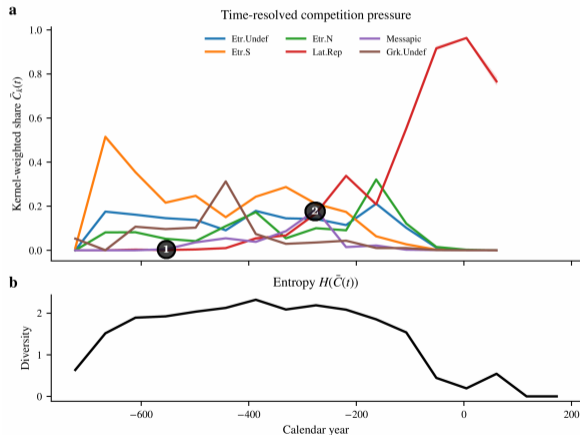


(a) Time-resolved competition pressure

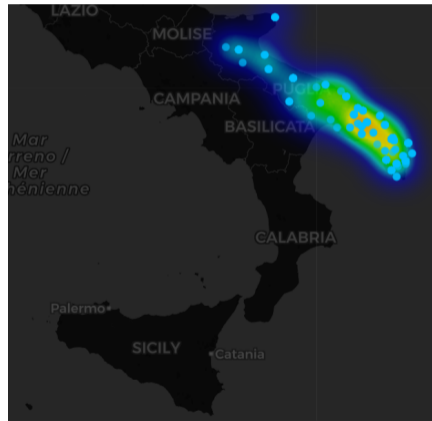


(b) Heatmap of inscriptions in the Greek alphabet

# Interpreting Alphabet Competition Over Time: Messapic Alphabet

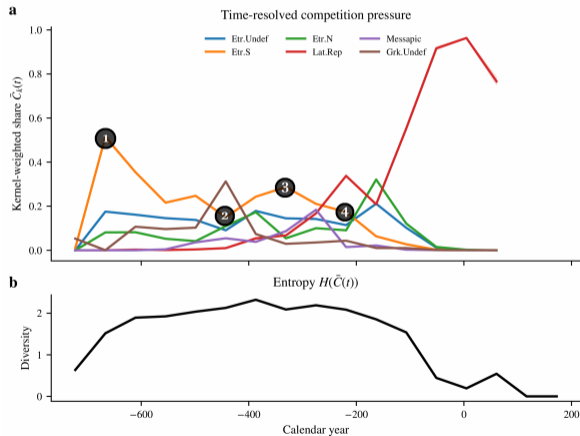


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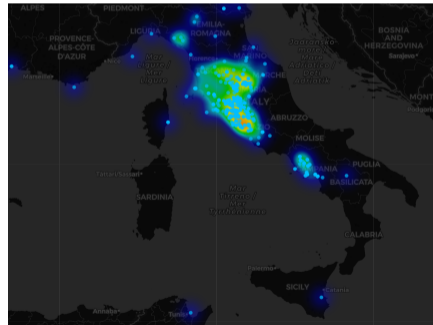


(b) Heatmap of inscriptions in the Messapic alphabet

# Interpreting Alphabet Competition Over Time: Southern Etruscan Alphabet

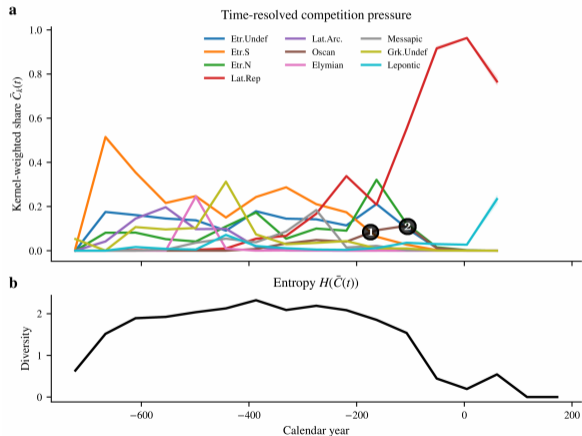


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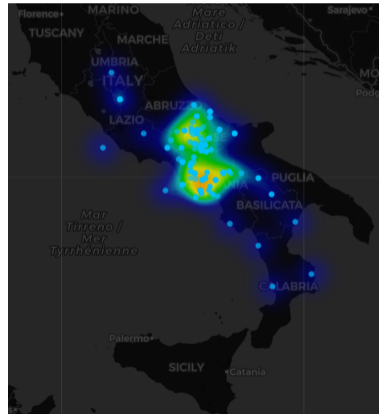


(b) Heatmap of inscriptions in the Southern Etruscan alphabet

# Interpreting Alphabet Competition Over Time: Southern Etruscan Alphabet and Oscan (not just Latin!)

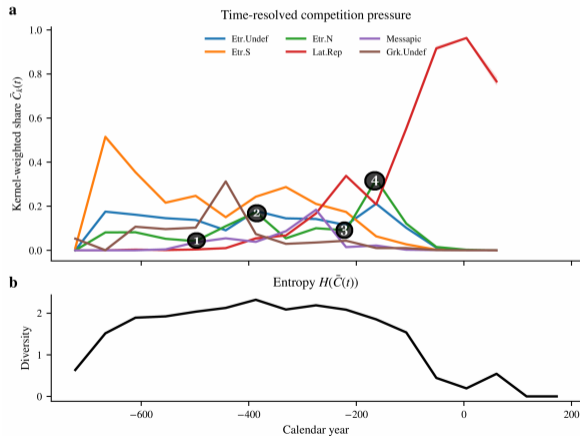


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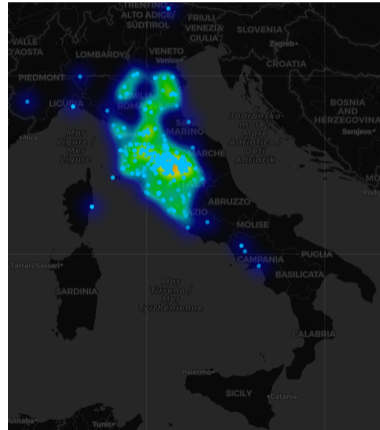


(b) Heatmap of inscriptions in the Oscan alphabet

# Interpreting Alphabet Competition Over Time: Northern Etruscan Alphabet

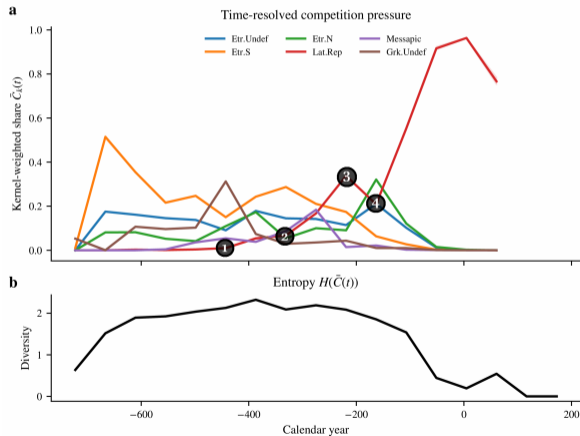


(a) Time-resolved competition pressure

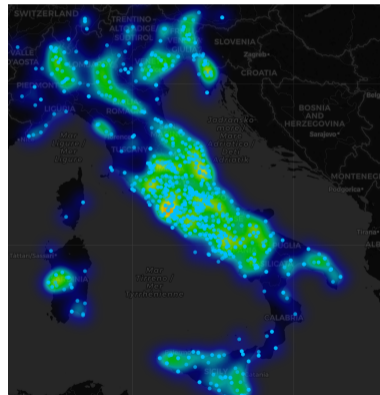


(b) Heatmap of inscriptions in the Northern Etruscan alphabet

# Interpreting Alphabet Competition Over Time: Latin Alphabet



(a) Time-resolved competition pressure



(b) Heatmap of inscriptions in the Latin alphabet

# Model performance

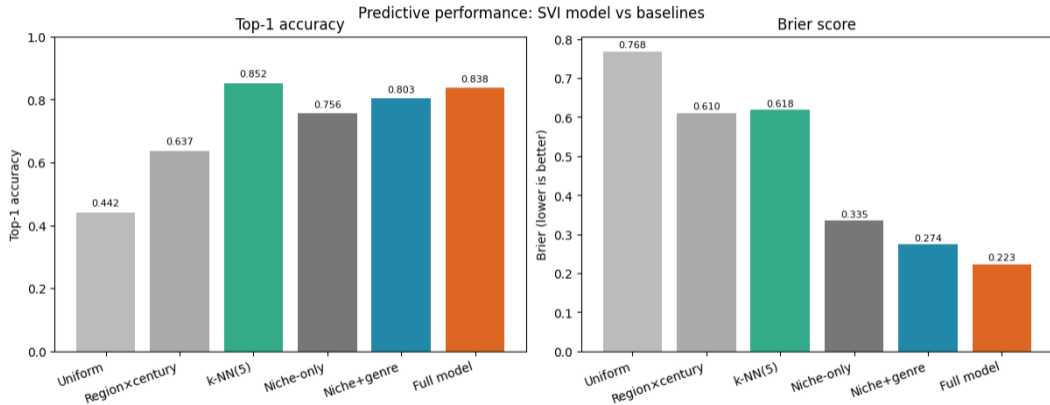
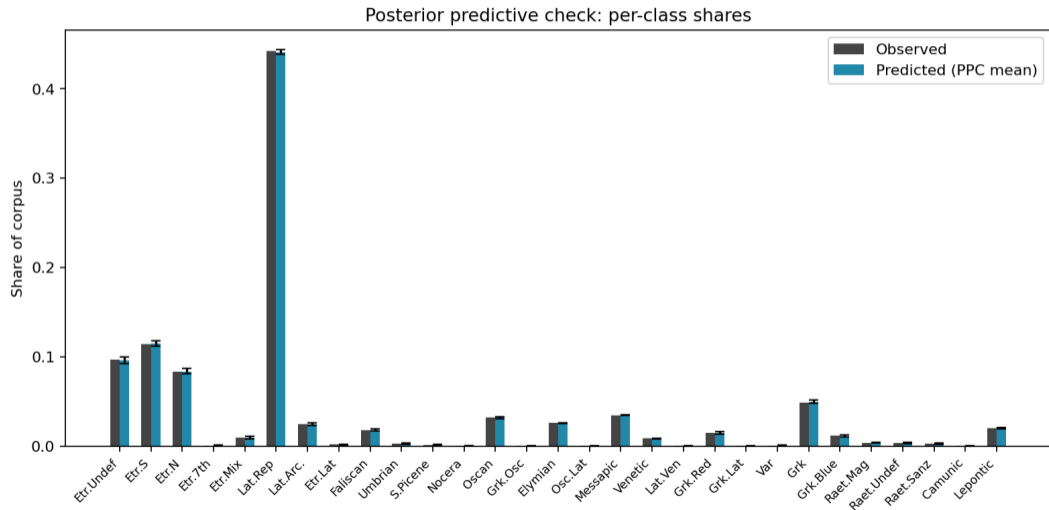


Figure: Prediction accuracy and error

# Posterior predictive checks



## Conclusions

- Roman conquest does explain *some* changes in alphabet competition, but colonization efforts and migration by several other actors (including Punics, Greeks, Syracusans, Oscans, Etruscans, etc.) are also essential for understanding alphabet dynamics in 1<sup>st</sup> millennium BCE.

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- The privileging of literary texts perpetuates ancient Greco-Roman narratives and silences the voices of the other groups of language speakers in Italy whose voice is recorded in the vibrant multi-lingual inscriptional record.

## Future work

- **Date-uncertainty in the kernel.** In contrast to the spatiotemporal effects, the competition kernel uses midpoint  $t$ . We could instead use an  $n$ -node Gauss–Legendre quadrature over  $\text{Uniform}(a_i, b_i)$  or some other prior distribution.

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- **North Africa and Phoenician/Punic.** Languages from Italy end up in the North African inscriptional record: what interactions can be observed there?






**Thank you for listening!**

Comments? Questions?






## References I

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